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Evaluation of SLAR and Thematic Mapper MSS Data for Forest Cover Mapping Using Computer-Aided Analysis Techniques

> ORIGINAL PAGE 12 OF POOR QUALITY

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I. ACTIVITIES OF THE PAST QUARTER

A. Data Collection

1. Radar Data Collection and Evaluation

The radar mission, Mission Number 424, was successfully flown on June 30, 1980. This was the first radar data to be obtained in support of the current project. The sensor used was the APQ-102 side-looking radar, and the aircraft platform was the WB-57F flown at an average altitude of approximately 60,200 feet MSL. Small scale color IR photography was also obtained of the study site as part of this mission.

The APQ-102 side-looking radar is a fully focused synthetic aperature radar imaging system. A horizontally polarized pulse of energy of 9600 MHz + 5 MHz (this wavelength band is commonly known as X-Band) was transmitted by the radar system, and the returning energy was recorded on separate holograms as horizontally (HH) and vertically (HV) polarized responses. These holograms were then processed through an optical correlator and the resulting images recorded on positive film, which was the format in which the data were provided by NASA to LARS.

The positive-map film was received at LARS on August 8, 1980. Black and white negatives and positive prints were then made of the radar film for handling and pre-analysis purposes.

Visual comparison of the HH images and HV images indicates that there is a distinct dark band in the imagery which covers about 30 percent of the radar strip (see Figure 1). This band is very distinct on the HH images and is also quite noticeable on the HV images. Because the dark band falls on the test site for the Flight Line 2 data, the value of a detailed quantitative analysis of Flight Line 2 appears questionable (see Figure 2). However, the Flight Line 1 data looks reasonably good and the dark streak does not fall on the test site area, so this should provide a good data set for the quantitative analysis. Preliminary evaluation of the data indicates that various features on the HH and HV images seem to give different response levels, which provides promise for using this type of data to differentiate among various cover types and/or condition classes. This aspect of the data will be carefully studied.

The amount of sidelap due to the look-angle between Flight Lines 1 and 2 is negligible. This was surprising, since the flightline centers were defined to be only 5 n.mi. apart, but the swath width of the APQ-102 is 10 n.mi. Examination of the imagery indicated that the start (south end) of Flight Line 1 was exactly where it should have been, but apparently there was some drift as the aircraft flew up the flightline, resulting in a smaller portion of the test site being imaged at the northern end of the flightline (Figure 1). Flight Line 2 was flown 1-2 n.mi. to the east of the desired location, resulting in the lack of overlapping data. The slight amount of sidelap that does exist falls on the very edge of the data where the image quality is too poor to be of use. Since there is no useful sidelap in the data, analysis of forest cover as a function of look-angle (using the overlapping area of the two flight lines) cannot be pursued with this data set.

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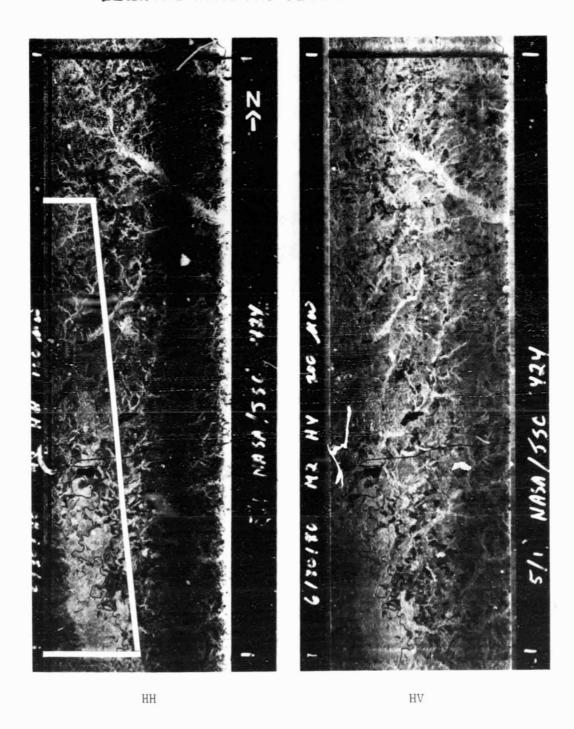


Figure 1. Radar images of flight line 1 for the HH and HV polarizations. The corresponding area of the MSS data is outlined in white.

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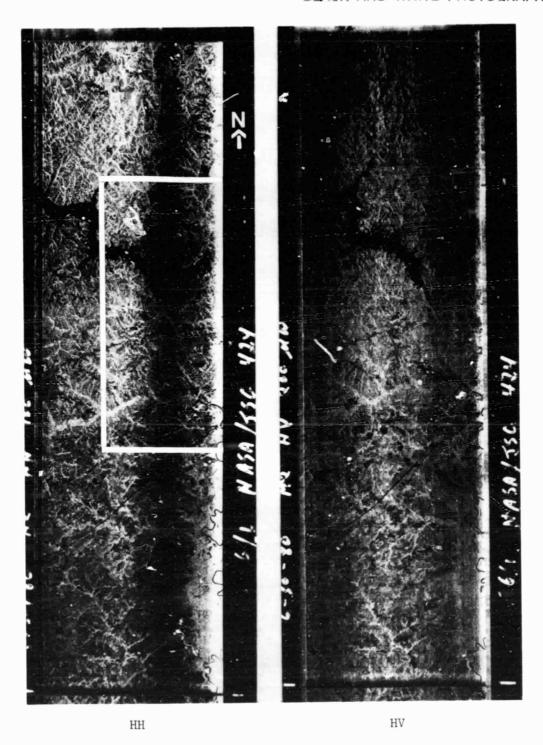


Figure 2. Radar images of flight line 2 for the HH and HV polarizations. The corresponding area of the MSS data is outlined in white.

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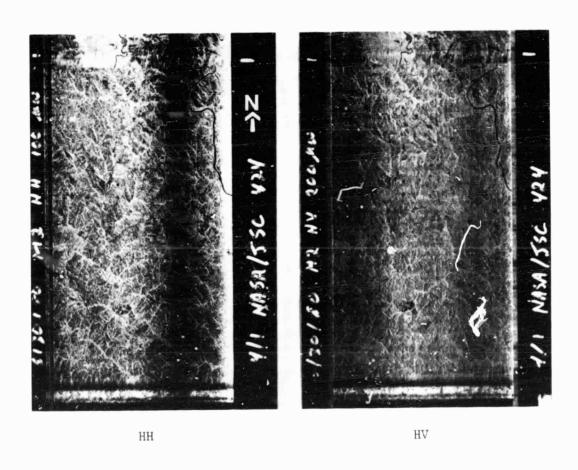


Figure 3. Radar images of flight line 3 for the HH and HV polarizations.

An estimation of the scale in the "along-track" and "across-track" directions indicates that there could be a significant difference between them. The scales were determined by measuring the distance between two points on the radar images and the same two points on USGS maps; two different measurements were taken for each direction and the averages com-The approximate scale for the along-track direction is 1:361.000 and the across-track direction is 1:413,000. Normally on fully focused SAR systems the along-track and across-track scales are the same (Tomiyasu, 1978). This is because the length of the flight line over which the signals are combined is equivalent to the along-track length of the illuminated area at far range for any given pulse (Greer, 1975) . Because of this relationship many variables can influence both the along-track and across-track scales, and thus create significant differences between the scales even though the system is a fully focused SAR system. The SAR system is a phase-coherent system and the differences or phase errors can be attributed to system imperfections such as radar-platform velocity deviations, targets in motion, electromagnetic path length fluctuations, and electronic equipment instabilities (Tomiyasu, 1978) . Since spatial characteristics, such as resolution and swath width, of the radar system are based on the same properties used to determine the scale, the system parameters must be evaluated to make an accurate determination of the spatial characteristics of this data set.

2. Multispectral Scanner Data Collection

NASA Flight Mission #425 to obtain three flightlines of NS-001 MSS data and supporting aerial photography was successfully flown on July 2, 1980. A summary of the support data is shown in Table 1 along with characteristics of the camera equipment used.

The Flight Line 3 data quality was very good and virtually cloud-free. Flight Lines 1 and 2 both contained some cloud cover especially in the northern sections and near the city of Camden, South Carolina and over the adjacent Wateree Reservoir. Flight Line 1 over Camden and north of the city contained between 30% and 40% cloud cover while south of Camden the cover was only between 0% and 10%. The quality of Flight Line 2 was generally better than on Flight Line 1 and contained only between 10% and 20% cloud cover north of and over Wateree Reservoir.

Mission #425 was continued on July 3 in an attempt to collect scanner data over Flight Lines 1 and 2 under more favorable weather conditions. The weather was generally very hazy, however, and in some areas over 50% of the imagery was covered by either haze or cloud cover. This situation occurred both north of Camden on Flight Line 1 and north of the Wateree Reservoir on Flight Line 2.

3. Field Trip to the Study Site

A field trip to the study area was conducted by Ellen Dean from July 1 to July 3 for the purposes of obtaining ground information concurrent with NASA Flight Missions #424 and #425, and to become better acquainted with the study site and the characteristics and variability of cover types.

14.6 (10) 36.9 (hi) 14.9 (10) 36.7 (hi)

14.8 (10) 36.7 (hi)

300

35

21.2

297

22

20.9

Table 1.

		•	Blackbody Temp ('C)	14.8 (10)
Fhotography Information: NASA Flight Mission #425			Ground Speed (mph)	299
Information: NASA			Line Hiles	35
tography		tude(kft)	MCD	20.9
		Altitud	MSL	21.4
table 1. NO-UUL Scanner and Aerlal	11ght)		Run Time	6, 30"
1 alone	Flight #18 July 2, 1980 18:22:40 (time of flight)		Flightline	П

21.4 21.7 6' 20" 3, 40"

Flight #19 July 3, 1980 14:52:35 (time of flight)

	ପ		OF PO	OR	Q	UAL	.M
•	3lackbody Temp (C)	15.7 (10) 32.7 (hi)	15.4 (10) 32.7 (hi)	Roll	Number	22	23
				Forward	Lap	209	209
	Ground Speed (mph)	285	270	Focal	Length	9	9
	_,				ASA	160	100
	Line Miles	35	35	Filter	Factor	2	2
de(ktt)	MSL MCD	21.0	21.1	Shutter	Speed	1/250	1/250
Altitu	WST	21.5	21.6	Filter	#2	36% T	36% T
	Run Time	6, 30"	6' 30"	Filter	#1	14	12
	۵l			Camera	Type	Zeiss	Zeiss
	Flightline		2	Film	Type	S0397(C)	S0193(CIR)

The first two days were spent in the field gathering reference information and color photographs of the various agricultural and forest cover types and conditions. These sites were located on aerial photographs from the previous NASA mission, Mission #399, noting the occurrence of any specific changes in the cover type. On July 3 a rental plane was flown over Flight Lines 1 and 2 at an altitude of approximately 900 feet above mean sea level and numerous aerial photographs were taken to be used in conjunction with other ancillary data to compare with data obtained from Missions #424 and #425. Subsequently these photographs were identified and labelled as to their corresponding positions on the CIR photos from Flight Mission #425.

To provide background information to use in the interpretation of the radar imagery, data on weather conditions was obtained for a period of one and two weeks prior to the flight missions (Table 2). This data was recorded at the Camden Weather Station, which is located in the camter of Flight Line 1.

B. DATA ANALYSIS

1. Selection of Test Fields

A COMTAL Vision One/20 display device was used to aid in selection and photo interpretation of the test fields for the various spatial resolutions being investigated. Blocks of the geometrically and "radiometrically" adjusted imagery (see Quarterly Progress Report September 1, 1979 - November 30, 1979 for discussion) were used.

The first step involved designing a test sample grid such that the cover classes occurring at the various coordinates of the coarser resolutions could be identified using data of only one resolution displayed on the COMTAL. By designing the grid such that the set of pixels examined for the test pixel identification corresponded exactly with the set of pixels averaged in the resolution degradation program, the identifications made using the finest resolution data could be precisely mapped into the coarser resolutions. The spacing for the grid is thus determined by the smallest number for which all resolutions provide a common denominator. Since, for the across-track dimension, the resolutions are the average of 1, 2, 3, and 4 pixels then the spacing for the grid in the across-track dimension which will allow us to map exactly between resolutions is 12. Similarly for the along-track grid spacings; the pixels averaged together for each resolution are 1, 2, 3, and 5. Hence, the grid spacing must be a multiple of 30. The grid was generated by GRID FTN (see Appendix B) for overlaying on the COMTAL image.

The COMTAL allows three different wavelength bands to be placed into separate image planes. These three planes can subsequently be assigned varying densities of red, green and blue colors, and overlaid to obtain a "truecolor" color composite image. This truecolor image was used, along with the ability of the COMTAL to magnify the image 1X, 2X or 4X, to accurately locate and identify the test fields. An example of this is shown in Figure 4 which displays one block of Flight Line 1 below Camden, South Carolina in magnification of 1X on which the Test Data Grid is overlaid. Figure 5 represents the central portion of the same scene at a 4X magnification.

Table 2. Weather Information from Camden, "outh Carolina

Date	Precipitation	(inches)	Temperatur (high)	e (°F) (low)	Relative Humidity (Kershaw Co.)
6/16	0.15				
%/17	0.15				
6/18	0.55				
6/19	none				
6/20	none				
6/21	nonê				
6/22	none				
6/23	trace		92	57	50%
6/24	0.7		90	68	-
6/25	1.37		90	68	-
6/26	trace		78	66	87%
6/27	none		82	62	58%
6/28	none		97	66	-
6/29	none		99	70	-
6/30	none		96	72	40%
7/1	none		98	64	41%
7/2	none		92	71	



Figure 4: A COMTAL Vision/One image of Flight-line 1-S south of Camden, S.C. The image is overlaid with the grid used to locate and evaluate the test fields.



Figure 5: A magnification of a portion of the same image as shown in Figure 4. Magnification to this scale was used for most of the interpretation and identification of test fields.

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Identification of the cover type in the test fields at all resolutions on the COMTAL was done in comparison with photo interpretation of the CIR photos. Identification into various cover types followed the format as outlined in the Quarterly Progress Report of June 1, 1979 - August 31, 1979, except for an additional class of tupelo which was found to be both visually and spectrally separable. All test fields at the various resolutions were evaluated separately and any border test fields, i.e., pixels containing more than one cover type at a particular resolution, were excluded from the final data set. The COMTAL coordinates and the test point identifications were recorded for subsequent translation into MIST coordinates for each resolution. This work has been completed for Flight Line 1-S. Blocks in Flight Lines 1-N and 2-N are currently being analyzed.

2. Wavehard Combination Evaluation

Much of the work conducted in waveband combination evaluation for this project is discussed in a paper prepared for presentation at the Fall Technical Convention of the American Society of Photogrammetry. A copy of this paper is included as Appendix A. Review of that article prior to reading the following text is suggested, as duplication is avoided wherever possible. However, there were several considerations and activities of the work that were not reported in the appended paper. The following discussions will focus primarily on these details of the analysis.

The a priori estimation of the probability of correct classification employing a measure of statistical difference between spectral classes relies heavily on: 1) the degree to which the group of class densities represent the distributions of spectral response vectors associated with each cover class (Swain, 1978) and 2) the degree to which the set of class densities is exhaustive of the range provided by the response vectors from the area to be classified (Wiersma and Landgrebe, 1979). If the class densities satisfy the above conditions, then statistical separability of the class densities should provide a fairly reliable estimate of percent correct classification.

The actual computation of transformed divergence, as well as the vast majority of other "separability" measures, involves only two class densities for each individual computation or value. Transformed divergence is thus a measure deemed appropriate for a two class case of equal a priori probability. A problem arises when such a measure is to be employed to provide an estimate of overall percent correct classification involving a multiple of spectral classes of unequal a priori probabilities. This problem is further compounded by the fact that subsets of these classes represent different cover classes. 1/
The averaged transformed divergence is given by:

$$TD_{ave} = \frac{1}{n} \sum_{k=1}^{n} TD_k$$
 (1)

for n number of spectral class pairs.

^{1/}The need to provide estimates for only relative percent correct classifications for purposes of ranking possible waveband combinations does not alleviate the problem.

However, the relative frequency of each spectral class pair is assumed constant in such an approach. This is rarely the case.

An unweighted, arithmetic average of all TD-values will result in the separability of two infrequently occurring classes having equal impact on the percent correct classification estimate, as the separability of two common classes. Consider the following:

Given a probability space S, $s_{ij} \in S$, i = 1, ..., k - 1, j = i + 1, ..., k for each j, where k = the total number of spectral classes. If each s_{ij} is considered the simultaneous occurrence of each spectral class of the pair $(s_i \text{ and } s_j)$, the occurrence of each being independent of the other, then the probability of the occurrence of the "spectral class pair" can be determined by:

$$W(s_{ij}) = P(s_i) P(s_j); (s_i n s_j) = \emptyset$$
 (2)

W(S₁₁) is a weight, distinct from the probability associated with an occurrence. To ease the complexity of indexing, it is assumed here that each cover class is represented by only one spectral class. The computations are easily extended into the case where the number of spectral classes in each cover class is greater than one. Then an unbiased estimator of averaged transformed divergence, corresponding more closely to probability of correct classification is given by:

$$TD_{ave} = \sum_{i=1}^{k-1} \sum_{j=i+1}^{k} W(s_{ij}) TD_{ij}$$
(3)

These probabilities should be treated with caution, as they are directed merely at extending the application of statistical distance as an estimator of probability of correct classification from the two class case to the multi-class case. The above presentation also assumes the availability of estimates of the $P(s_i)$ and $P(s_i)$. These are empirically derived using the relative frequency of each spectral class in each cover class and the relative frequency of each cover class. Computationally:

$$P(s_i) = P(s_i/C_\alpha) P(C_\alpha) \quad \alpha = 1, \dots, m$$
 (4)

where: P(C) is given by the total number of pixels in the training data in cover class α divided by the total number of pixels from all cover classes in the training data.

 $P(s_{\alpha}/C_{\alpha})$ is given by the total number of pixels in the training data spectral class s_{α} , which is a subset of C_{α} , divided by the total number of pixels in cover class C_{α} . 2/

As may well be apparent, the algebraic identify of these probability estimates provides a computational shortcut to the probabilities of interest.

While these frequencies are easily obtained, their use in providing unbiased estimations of the above probabilities is dependent on each observation being randomly selected. That is, the selection of each additional pixel in developing the training data is completely at random. While this is rarely the case, the extent to which this assumption is violated will erode the "goodness" of each P(s;) and hence the resulting TD . This has been used by some researchers as the rationale for not weighting each observed TD, and employing the unweighted arithmetic mean in the multiclass case.

If while this may well be warranted in many cases, it must be reconciled that weights are always employed. Where they are not computed and employed in the summation, they are merely assumed equal. Obviously,

$$\frac{1}{n} \sum_{k=1}^{n} TD_k = \sum_{k=1}^{n} \frac{1}{n} TD_k$$
 (5)

The problem then becomes one of assuming some set of population parameters $(x_1, x_2, x_3, \ldots, x_k)$ where k is the number of spectral classes contained in the population and the x_i are the total number of pixels belonging to each ith spectral class. The actual probabilities are then,

$$P(x_i) = x_i \begin{bmatrix} x \\ y = 1 \end{bmatrix}^{-1}$$
 (6)

Then, for the weighted as opposed to the unweighted case:

$$E_{1} = \sum_{i=1}^{k} |\hat{P}(x_{i}) - P(x_{i})|$$
 (7)

and

$$E_{2} = \sum_{i=1}^{k} \left| \frac{1}{k} - P(x_{i}) \right|$$
 (8)

where \mathbf{E}_1 is the error for the weighted case and \mathbf{E}_2 is the error for the unweighted case,

is
$$E_1 \geq E_2$$
 ?

This is the consideration which, in spite of not being testable, must be resolved before proceeding with any multiclass case employing averaged statistical distances. While an in-depth evaluation of this proble is beyond the scope of this study, the evaluation of waveband combinations employing the weighted average was considered imperative for complete treatment of this part of the study. Table 3 provides a rank ordering of channel combinations for each waveband combination level for the weighted mean TD-values.

The work in waveband combination evaluation prompted the development of several programs which were written to be compatible with LARSYS. These are listed in Appendix B with brief descriptions.

Among these was a program which computed average transform divergence over all spectral class pairs for each cover class pair and over all spectral class pairs for each cover class. The tables of these results are shown in Appendix C, and provide insight as to the dependency of waveband combination rank on cover class composition of the area to be classified. Such output will also assist individual users of diverse interest to select those waveband combinations most suited to their particular application. By electing that waveband combination of maximum TD in cover classes with which they are concerned, the classifier can be "fine-tuned" according to the users needs. The disagreement between max(TD ave) by cover class, cover class pair, and overall cover classes is very common.

Separability by cover class pairs will also provide information on which cover classes may require additional spectral classes in order to reduce their variance. It will also give an estimate of the results to be expected in the omission-commission error matrix.

3. Spatial Resolution Evaluation

The development of test statistics have been completed for the southern half of the easternmost flight line (Flight Line 1-S) for all resolutions (i.e., 15x15, 30x30, 45x45 and 60x75 meter data sets). Prior to generating all of the statdecks for each resolution, an evaluation of the spectral classes for the 30 meter data was conducted by classifying the training fields.

As indicated in the paper included as Appendix A, statistics for each class density were provided by a supervised cluster approach. The line-column coordinates of supervised samples of each cover class were identified from the COMTAL Vision One/29. These coordinates were translated into MIST coordinates and a LARS-12 card deck was generated by CAGEN2 FORTRAN (see Appendix B). These were then sorted by cover class and separate cluster analyses were run for each cover class. The individual statistics decks were merged, providing 32 spectral classes for 12 cover classes. Table 4 contains the resulting class parameters by spectral class, by cover class.

Separability indicated that these class densities were on the average, very separable and that acceptable classification accuracies could be expected. However, in order for class densities to provide high classification accuracies the classes must be:

- representative of the distribution of observations of the same class,
- 2) separable or distinguishable among all other classes,
- 3) exhaustive of the sample space from which observations are drawn.

Table 3. Rank Ordering of Best Seven Channel Combinations for each Channel Combination level (ordering criterion is Average Transformed Divergence over all spectral class pairs).

1	<u>2</u>	<u>3</u>	4	<u>5</u>	<u>6</u>
6	3,4	3,4,5	1,3,4,5	1,2,3,5,6	1,2,3,4,5,6
3	3,5	3,4,6	3,4,5,6	1,2,3,4,6	1,2,3,5,6,7
4	2,4	3,5,6	1,3,4,6	1,2,3,4,5	1,2,3,4,6,7
5	4,6	2,4,5	2,3,4,6	1,3,4,5,6	1,2,3,4,5,7
1	3,6	1,3,4	2,3,4,5	2,3,4,5,6	1,2,4,5,6,7
2	2,5	2,4,6	2,3,5,6	1,2,4,5,7	2,3,4,5,6,7
7	5,6	2,5,6	2,4,5,6	1,2,4,5,6	1,3,4,5,6,7

Note: Channel 1 = $0.45 - 0.52 \mu m$

Channel 2 = $0.52 - 0.60 \mu m$

Channel 3 = $0.63 - 0.69 \mu m$

Channel 4 = $0.76 - 0.90 \mu m$

Channel 5 = $1.00 - 1.30 \mu m$

Channel 6 = $1.55 - 1.75 \mu m$

Channel 7 = $10.4 - 12.5 \mu m$

Table 4 . Summary of Statdeck Containing 32 Spectral Classes.*

	<u>1</u>	<u>.2</u>	<u>3</u>	4	<u>5</u>	<u>6</u>	<u>7</u>
SOTL1	154.87	177.14	199.76	131.14	188.11	189.22	143.31
	243.34	635.95	755.00	320.86	308.40	513.50	757.91
SOILZ	129.42	125.67	128.85	135.62	144.49	144.83	139.44
	34.26	194.42	240.09	223.42	158.03	158.41	1162.87
SOTL3	111.10	95.43	92.80	99.29	109.41	106.21	135.06
	105.86	235.72	398.18	361.95	331.33	396.72	734.38
PAST1	93.94	74.46	62.05	118.41	122.58	91.51	137.99
	24.38	41.55	92.69	259.57	197.63	90.66	432.61
PASTS	87.89	65.24	44.09	155.37	135.89	68.69	95.19
	22.39	38.95	24.31	140.19	93.50	68.85	74.75
PAST3	85.36	61.38	42.37	119.42	106.93	57.08	30.27
	20.05	27.50	40.48	258.94	140.35	57.77	122.54
PAST4	96.11	72.86	57.77	38.39	31.09	22.08	45.94
	9.05	22.52	21.87	103.32	112.83	77.18	322.49
CROP1	117.55 42.54	111.12 130.55	100.67 309.76	172.25 203.03	161.50 140.88	119.55 229.87	103.02
CROP2	100.77	76.21 16.76	52.34 22.41	210.17 176.97	160.62 39.00	60.76 40.72	82.34 40.46
CROP3	99.82	82.30	71.21	118.67	117.97	91.50	137.56
	37.79	37.85	70.78	115.25	119.15	203.40	263.31
CP 1P4	96.03	76.84	59.45	150.22	127.02	64.76	97.05
	5.16	30.63	45.47	199.39	141.36	70.29	194.52
PINEI	92.26	69.76	54.05	113.46	115.17	71.85	116.23
	3.11	6.35	13.48	81.46	55.40	50.93	298.47
BINES	94.75 15.59	57.90 8.73	48.67 5.99	118.79 104.89	112.27	59.50 40.22	83.64 73.18
PIHD1	91.69 14.58	69.46 8.39	55.44 11.96	109.79 54.06	119.61	70.28 28.63	127.44 379.38
bIHDS	94.31 6.04	65.79 7.81	46.95	112.63 119.94	105.95 85.44	53.95 29.96	84.25 54.55
HDWD1	84.36	51.83	42.03	140.62	125.34	63.50	84.96
	9.19	19.05	14.24	228.86	171.32	67.09	98.88
HD#02	91.78	70.90	59.56	99.01	101.23	76.15	125.33
	24.90	47.12	121.63	010.36	911.00	579.66	909.75
SGHD1	91.42	57.31	44.23	175.67	150.73	71.57	84.74
	7.13	9.40	5.47	55.54	38.43	29.82	55.83
SCHD2	85.10	51.11	40.45	155.12	133.78	63.66	81.08
	32.01	20.54	5.09	54.63	29.75	17.06	80.84
SGHD3	91.52	64.64	41.91	131.63	112.29	56.05	68.85
	13.22	9.93	6.45	126.95	92.78	16.65	34.31
TUPE1	84.63	61.26	41.99	134.63	119.80	60.42	80.56
	4.51	12.07	15.19	366.89	253.77	69.31	146.03
TUPE2	78.38	50.18	38.94	44.15	45.85	35.99	112.04
	3.70	15.81	23.85	168.05	386.93	304.10	909.13
SYCAL	87.53 2.98	65.20 4.09	50.40 13.40	123.40	124.13 204.27	82.87 11.41	116.73 105.64
SYCAS	34.40 2.15	60.05 4.58	39.70 7.80	130.50	115.20 167.96	56.95 28.58	90.05 35.84

Table 4 . Summary of Statdeck Containing 32 Spectral Classes (cont'd.).

	<u>1</u>	<u>2</u>	3	4	<u>5</u>	<u>6</u>	<u>7</u>
CCUT1	99.74 47.58	82.77 106.86	83.39 286.95	91.37 384.24	297.92 297.92	102.02	136.91 167.45
CCUTS	84.78 17.53	63.53 36.59	44.63 43.53	141.22 238.84	128.27 127.66	69.31 81.24	93.55 197.84
MVEG1	102.64	79.12 73.10	65.19 174.96	110.00 54.54	123.25 51.46	89.91 102.11	123.56
MVEG2	100.76	76.83 20.02	52.67 14.56	123.72	112.42	64.49 66.70	80.16
TUWAI	172.62 107.95	195.82	139.18 79.42	55.29 94.48	37.92 120.65	27.02 25.07	76.42 28.94
VEGE 1	126.09 152.90	114.84 502.68	88.24 386.25	104.06	95.88 392.74	63.05 204.26	90.47 115.30
VFWA1	197.53 19.90	36.65	55.08 2 7. 39	61.83 119.81	57.93 111.52	42.91 59.06	88.04 29.35
WATRI	107.05 43.52	79.41 123.32	52.51 31.17	39.08 13.04	33.05 17.75	24.97 14.22	71.62 143.33

^{*}Within each spectral class, the upper element is the mean and the lower is the variance.

Channel Number	Band
1	0.45 - 0.52 μπ
2	0.52 - 0.60 μm
3	0.63 - 0.69 μπ
4	0.76 - 0.90 μπ
5	1.00 - 1.30 µm
6	1.55 - 1.75 µm
7	10.4 - 12.50 nm

The degree to which Condition 2 is met is indicated by TD ave or *SEPARABILITY. Condition 1 and 3 are truly only evaluated at the time of classification. However, Condition 1 can be partially evaluated by classifying the pixels contained in the training fields. While this "test" is only sensitive to the location of class densities in the q-variate hyperspace relative to the individual response levels, it is a very good means of testing whether these class densities correspond to "regions" of concentration as they exist in the data. This idea is confirmed by the change in spectral class variance for a cover class with respect to changes in the number of spectral classes.

The training fields were classified using a per-point Gaussian Maximum Likelihood (GML) classifier (a priori probabilities were assumed equal). The training classes were the 32 spectral classes presented in Table 4. The classification result using all seven channels (channel calibration code 7) is provided in Table 5. Overall classification was only 47.4%. Although these cover classes are fairly specific in nature, the reasons for the resulting accuracy level were investigated. Examining the error matrix indicates extremely low classification accuracies for pasture, hardwood, tupelo, sycamore, and clearcut. The number of spectral classes representing each of these categories are 3,2,2,2, and 2 respectively. By increasing the number of spectral classes (re-clustering with a greater number of cluster classes specified) to a total of 37 classes, an overall performance of (see Table 7) was attained. By comparing Table 4 and Table 6, the reason for improvement of this magnitude becomes apparent. The smallest reduction of variance for hardwood was a factor of 3.2 for Channel 1. The largest reduction in variance was a factor of 25 for Channel 6. Reductions in variance of this order indicate that the location of the cluster centers in the q-variate hyperspace deviated substantially from the actual "regions" of concentration in the data. The cluster centers were assumed to be located somewhere between such regions. A reduction in variance of similar magnitude occurred for tupelo. Smaller reductions occurred in pasture and clearcut. This is probably due to the highly variable states of nature found in conjunction with each of these latter cover classes, resulting in a more general spread in the distributions, with less pronounced concentrations in the data. When working with q-variate hyperspace, univariate histograms and bivariate scatterplots are not optimal but are essentially the only tools available to obtain some insight regarding the data distributions. Much attention was given to training statistics development since the concern in the later analyses will be with differences in classification accuracies achieved with different resolutions.

The persistently low classification accuracy for sycamore is due to:
1) extremely high similarity to second growth hardwoods and 2) the availability of a very small number of training pixels. This class has therefore been merged with second growth hardwood.

Training statistics for each of the spatial resolutions are currently being developed for the spatial resolution evaluation. It is anticipated that results for this part of the study will be available for the next report.

Classification Performance Evaluation from Classification of Training Data with 32 Class Training Statistics. Table 5.

	No.	•															
	or Pts.	Correct	Soil		Crop				Sghd				Mveg		Mveg	Vewa	Watr
Soil	1946	88.6	1724		22				0				6		9	7	1
Past	987	24.7	9		520				က				9		n	0	0
Crop	1445	98.1	9		1417				-				Т		7	0	0
Pine	805	81.4	0		0				0				4		0	0	0
Pihd	314	8.68	0		0				-				2		-	0	0
Hdwd	3997	5.1	0		7				2301				7		0	7	0
Sghd	2242	0.46	0		2				2107				н		0	7	0
Tupe	350	0.0	0	186	52	0	0	101	4	0	0	0	7	0	0	0	0
Syca	35	0.0	0		æ				20				-		0	0	0
Ccut	4277	17.9	234		40				33				32		7	11	-
Mveg	294	98.0	æ		0				0				288		0	0	0
Tuwa	124	99.2	0		0				0				0		H	0	0
Mveg	99	100.0	0		0				0				0		99	0	0
Vewa	39	97.4	0		0				0				0		т	38	0
Watr	232	97.0	0		0				0				0		0	0	225

Overall Classification Accuracy (8136/17153) = 47.4%

Table 6 . Summary of Statdeck Containing 37 Spectral Classes.*

	1	<u>2</u>	<u>3</u>	4	<u>5</u>	<u>6</u>	<u>7</u>
SOTL1	154.87 243.34	177.14 635.95	169.70 705.00	131.14	188.11 308.40	189.22 513.50	143.31 767.91
SOILS	128.42 33.25	125.67 194.42	128.85 240.09	135.62	144.49 158.03	144.83 158.41	139.44 1152.67
S01L3	111.10 105.86	95.63 235.72	92.EN 308.13	99.29 361.95	109.41 331.33	106.21 356.72	135.06 734.38
PAST1	107.48	93.05 24.30	21.10 74.74	148.14 151.33	162.16 87.59	131.79 63.29	197.08 283.63
P4ST2	134.55	85.95 9.49	62.46 17.70	184.67 116.83	176.23 34.90	102.77	145.38 138.17
F1249	104.30 19.73	85.04 22.34	69.62 52.99	141.63 152.09	148.91 27.33	105.70 c8.25	154.41 196.43
PAST4	99.52 8.07	39.96 13.68	58.73 17.95	171.73	154.55 59.75	d4.27 35.41	115.33 58.16
PAST5	97.60 5.56	73.76 7.60	51.20 7.15	165.09	135.90 30.41	63.37 25.35	97.51 55.28
CROP1	117.65 42.54	111.12 130.55	100.67 309.76	172.25 203.03	161.50 140.88	119.55	103.02
CBUBS	100.77 5.80	76.21 16.76	52.34 22.41	210.17 176.97	160.52 39.00	08.76 40.72	82.34 40.46
CR1P3	99.82 37.79	32.30 37.85	71.21 70.78	118.67 115.25	117.97 116.15	203.40	137.56 268.31
CROP4	96.08 6.16	76.64 30.63	58.45 45.40	150.22 199.89	127.02 141.36	64.76 70.27	97.05 194.62
PINEI	92.26 3.11	69.76 6.35	54.05 13.46	113.46	115.17 65.40	71.80 50.93	116.23 288.47
BINES	94.75 15.59	67.90 8.73	49.67 5.99	118.79 104.89	112.27 83.45	59.63 40.22	83.64 73.18
bInD]	91.69 14.58	69.46	55.44 11.85	109.79	110.61	70.28 48.53	127.44 379.38
ьІнύS	94.31	65.79 7.61	45.99 7.69	117.63	105.95 35.44	53.95 29.96	84.25 54.55
нрмо1	92.12	66.21 4.29	43.92 2.64	161.01 33.25	138.32 20.72	65.29 15.45	78.90 30.02
HC≒DS	91.45 4.73	66.07 11.20	43.94 5.93	146.15 30.91	127.10 15.15	61.57 13.43	77.05 43.73
нрирз	94.52 9.75	58.21 7.59	38.78 5.89	124.69 36.81	105.22	52.82 10.90	72.92 19.29
SGHD]	91.42 7.13	67.31 9.40	44.23 5.47	175.67 55.54	150.73 38.43	71.57 29.82	94.74 55.83
SGHDZ	86.10 32.01	61.11 20.54	49.45 6.09	155.12 54.63	133.78 29.75	63.65 17.06	81.08 80.84
2èhù3	91.52 13.22	64.64	+1.91 6.45	131.63	112.29 92.78	56.05 16.65	65.85 34.31
TUPEl	95.44 7.53	80.55 12.71	51.29 3.64	193.49 66.36	155.89 30.81	77.26 10.74	80.27 97.30
TUPEZ	95.67 7.47	80.57 12.79	51.68 4.47	154.41 45.11	141.59 36.50	74.91 12.20	81.98 37.88

Table 6. Summary of Statdeck Containing 37 Spectral Classes (cont'd.).

	1	<u>2</u>	<u>3</u>	4	<u>5</u>	<u>6</u>	<u>7</u>
TUPE3	82.83 8.41	72.n7 3.40	46.51 U.89	124.39 11.67	109.04	60.90 1.50	79.67 22.23
SYCA1	67.53 2.98	66.20 4.39	50.40 13.40	123.40 358.47	124.13 204.27	82.37 11.41	116.73 105.54
SAC25	34.40 2.15	40.65 4.58	39.70	130.50 294.47	115.20 157.96	56.95 28.55	30.05 35.84
CCUT1	101.66	33.29 50.10	73.24 145.27	121.39 163.30	135.02 73.32	112.71 123.54	189.76 463.75
CCUT2	96.86 17.11	76.45 35.73	64.94 117.13	107.61 191.37	114.36 140.05	91.23 98.60	137.69 198.27
CCUT3	91.66 7.20	70.97 11.70	50.25 19.19	142.64 276.54	131.36 110.55	77.78 44.09	100.85 132.54
CCUT4	91.17 19.28	56.36 26.99	52.46 75.15	83.56 330.60	83.20 325.53	62.04 164.53	98.73 300.15
MVEG1	102.64	79.12 73.10	65.10 174.96	110.00 59.84	123.25 51.46	89.31 102.11	123.56 204.00
MVEG2	100.76	76.83 20.02	52.67 14.56	123.72 173.99	112.42 118.27	64.49 05.70	80.16 113.35
TUWA1	172.62 107.95	195.52 279.16	139.18 79.42	55.29 94.48	37.92 120.65	27.02 95.07	75.42 28.94
VEGE1	126.08 152.50	114.84 502.66	88.24 386.20	104.06	95.88 392.74	63.05 20+.28	90.47 115.30
VFW41	107.63	32.53 35.65	55.08 27.39	51.63 119.81	57.93 111.52	42.91 59.06	89.04 29.35
WATRI	107.08 43.52	78.41 123.32	52.51 31.19	39.08 13.04	33.06 17.75	24.97 14.22	71.62 143.33

*Within each spectral class, the upper element is the mean and the lower is the variance.

Channel Number	Band
1	0.45 - 0.52
2	0.52 - 0.60
3	0.63 - 0.69
4	0.76 - 0.90
5	1.00 - 1.30
6	1.55 - 1.75
7	10.4 - 12.50

Classification Performance Evaluation from Classification of Training Data with 37 Class Training Statistics. Table 7.

	No.	3 -1															
	Pts.	Correct	Soil	Past	Crop	Pine	Pihd	Hdwd	Sghd	Tupe	Syca	Ccut	Mveg	Tuwa	Vege	Vewa	Watr
Soil	1946	95.3	1855	e	22	7	7	0	0	0	0	97	7	-	9	7	7
Past	987		S	776	œ	0	0	0	-	ပ	0	29	0	0	0	0	0
Crop	1445	97.0	6	23 1	1402	2	-	0	7	0	0	'n	7	0	7	0	0
Pine	805		H		0	653	124	4	0	0	0	19	4	0	0	0	0
Pihd	314		0			26	282	H	0	0	0	7	2	0	-	0	0
Hdwd	3997		0			-	10	3507	357	2	37	75	4	0	0	0	0
Sghd	2242		0		2	0	0	307	1907	9	-	16	-	0	0	7	0
Tupe	350		0			0	0	7	0	346	0	0	7	0	0	0	0
Syca	35		0		0	0	0	0	20	11	0	ო	Н	0	0	0	0
Ccut	4277		147			107	2	82	22	39	25	3693	15	0	1	4	г
Mveg	294		m			2	0	0	0	C	0	7	287	0	0	0	0
Tuwa	124		0			0	0	0	0	0	0	0	0	123	-	0	0
Vege	99		0		0	0	0	0	0	0	0	0	0	0	99	0	0
Vewa	39		0			0	0	0	0	0	0	0	0	0	7	38	0
Watr	232		0			0	0	0	0	0	0	0	0	0	0	0	232

Overall Classification Accuracy (15335/17153) = 89.4%

TT. PROBLEMS ENCOUNTERED

No problems of significance were encountered during the past quarter. Some difficulties were encountered in following the methodology initially established for identification of the cover type in the defined test pixel, thereby causing some delay in the analysis of the 1979 TMS data. However, these problems have been resolved, and the modified methodology currently being used is much faster and should produce test data sets having a higher degree of reliability among the different analysts involved.

III. PERSONNEL STATUS

The following personnel committed the respective percentages of time to the project during the past quarter:

Name	Position	Ave. Monthly Effort (%)
Bartolucci, Luis	Professional Research Analyst	10
Dean, Ellen	Research Associate	100
Frazee, Michael	Research Assistant	50
Hoffer, Roger	Principal Investigator	80
Knowlton, Douglas	Research Associate	50
Latty, Rick	Research Associate	100
Peterson, John	Associate Director	5
Prather, Brenda	Secretary	50
Stiles, Stephanie	Secretary	3

TV. ANTICIPATED ACCOMPLISHMENTS

The following are the anticipated accomplishments of the forthcoming quarter (September 1, 1980 - November 30, 1980):

- Digitization of the SAR data for Flight Line #1, HH and HV polarizations.
- 2) Completion of the definition of the test data sets for Study Site 1-N and 2-N.
- 3) Continuation of the analysis of the four different spatial resolutions of the 1979 data.
- 4) Continuation of the analysis of the spectral characteristics of the 1979 TMS data.
- 5) Receipt of the 1980 TMS data and initiation of the reformatting and rectification procedures.

- 6) Prepare the 18-month report required by this contract.
- 7) Definition of the Statement-of-Work to be followed during F.Y. '81 and renegotiation of the contract for F.Y. '81.

No major technical problems are anticipated during the forthcoming quarter. Due to (a) an announced plan to significantly decrease the level of funding on this contract during F.Y. '81, and (b) the delays in obtaining, and characteristics of the TMS and SAR data obtained in support of this project, it is anticipated that the objectives initially proposed will need to be modified. These modifications will be reflected in the Statement-of-Work which will be developed during this next quarter.

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APPENDIX A

Paper entitled "Waveband Evaluation of Proposed Thematic Mapper in Forest Cover Classification," by R. S. Latty and R. M. Hoffer, to be presented at the 1980 Fall Technical Convention of the American Society of Photogrammetry, to be held in Niagara Falls, New York.

ORIGINAL PAGE IS

WAVEBAND EVALUATION OF PROPOSED THEMATIC MAPPER
IN FOREST COVER CLASSIFICATION

Richard S. Latty and Roger M. Hoffer Purdue University West Lafayette, Indiana 479

ABSTRACT

This study involved the evaluation of the characteristics of multispectral scanner data relative to forest cover type mapping, using NASA's NS-001 multispectral scanner to simulate the proposed Thematic Mapper (TM). The objectives were to determine: (1) the optimum number of wavebands to utilize in computer classifications of TM data; (2) which channel combinations provide the highest expected classification accuracy; and (3) the relative merit of each channel in the context of the cover classes examined. Transformed divergence was used as a measure of statistical distance between spectral class densities associated with each of twelve cover classes. The maximum overall mean pair-wise transformed divergence was used as the basis for evaluating all possible waveband combinations available for use in computer-assisted forest cover classifications.

INTRODUCTION

Early work in leaf spectra analysis (Billings and Morris, 1951; Gates and Tantraporn, 1952; Gates, et al., 1965; Gausman, et al., 1969; Knipling, 1970; Wooley, 1971; Gausman, 1977) provided much of the initial understanding of the variations in the amount of radiant energy returned from vegetated surfaces. Colwell (1974) identified the value of hemispheric leaf reflectance as only one of several important parameters responsible for these variations, and cautioned against making inferences about scene reflectance from leaf spectra information alone. Plant canopy modeling efforts (Idso and De Wit, 1970; Nilson, 1971; Oliver and Smith, 1972; Smits, 1972; Colwell, 1973) have identified many of the parameters which account for variations in the amount of radiant energy returned from the scene. The sel ation of waveband combinations which will provide acc rate classification of the various earth surface feat res requires an understanding of the reflective characteristics of those features relative to the various wavebands available. Properties of the data consequential to classification accuracy are not dependent solely on earth surface, atmospheric, and illumination conditions. They are also very dependent on the parameters of the sensor system to be employed (Silva, 1978). Therefore, the need exists to investigate these reflective properties employing data more closely simulating the data which will ultimately be employed for such classifications.

With parametric classifiers, the resulting classification accuracy is dependent on (1) the degree to which the

training classes (i.e., spectral classes) represent the spectral variability of their respective cover classes, and (2) the level of statistical "separability" among the training classes (Swain, 1978). The first condition is difficult if not impossible to assess without conducting the actual classification - the expense of which precludes evaluating many different waveband combinations. One can justifiably assume that the first condition is satisfied if the points providing the data for establishing the training classes are randomly generated, and are "sufficient" in number for each class relative to the number of wavebands employed. The number of samples statistically sufficient for the development of training classes increases exponentially with an increase in the number of channels employed in classification (Duda and Hart; 1973). Duda and Hart (1973) pointed out that, "beyond a certain point, the inclusion of additional features leads to worse rather than better performance." They provide an excellent review of the problem. This problem has also been examined by Allais (1966), Dynkin (1961), Fukunaga and Kessell (1971), Kanal and Chandrasekaran (1971) and others. The level of statistical "separability" can be computed from the mean vectors and covariance matrices associated with each of the training classes employing one of several statistical distance measures (Kailath, 1967; Swain, Robertson and Wacker, 1971; Wacker and Landgrebe, 1972; King and Swain, 1973).

METHODS AND ANALYSIS

Data Acquisition
The data were obtained on May 2, 1979 from the NASA NC-130 alreraft flying at an altitude of 20,000 ft. (MGD) over an area immediately south of Camden, South Carolina. The multispectral scanner (MSS) data were obtained by the NASA NS-001 multispectral scanner. (Table 1 shows the NS-001 scanner specifications as compared to the Thematic Mapper). Color and color infrared photographs (1:40,000 scale transparencies) were obtained at the same time. Cloud coverage was minimal and atmospheric conditions were considered excellent.

Data Handling and Preprocessing
The across track change in scale of the imagery was adequately reduced by employing a geometric model which describes the ground resolution element dimensions as a function of aircraft altitude, IFOV (instantaneous field-of-view) of the scanner, and change in scan angle corresponding to the analog signal integration interval.

A study of the data quality revealed an apparent correlation between scan angle and response level (different for each channel). The relationships appeared to be sufficiently high to obscure sources of variation otherwise correlated with differences between cover classes. Therefore, an empirically derived function was generated which described the variation in response level by column (corresponding with scan angle). Data were employed from areas where no

apparent stratification of cover class by column was present.* The shape of these functions were evaluated against both empirical (Anuta and Strahorn, 1973; Landgrebe, Beihl, and Simmons, 1977) and theoretical work (Kondratyev, 1969; Jurica and Murray, 1973) prior to actual response level adjustment. The final data product was considered appropriate for the analysis.

Table 1. Comparison of the NASA NS-001 multispectral scanner and the proposed Thematic Mapper (TM).

WS-001 Multispectral Scanner (1)

Proposed Thematic Marper (2)

Channel		Low Level Input (W-CM ⁻² ·SR ⁻¹)	MEap	Channel	•	(W-CM ⁻² .sR ⁻¹)	HEAP
1	0.45-0.52	0.7 x 10 ⁻⁶	0.5%	1	0.45-0.52	2.0 x 10 ⁻⁴	0.01
2	0.52-0.60	6.0 x 30 ⁻⁶	0.5L	2	0.52-0.60	2.4 x 10 ⁻⁴	0.56
•	0.63-0.69	5.0 x 10 ⁻⁶	0.54	,	0.63-0.69	1.3 x 10 ⁻⁴	0.58
4	0.76-0.90	4.4 x 10 ⁻⁶	0.5k		0.76-0.90	1.6 x 10 ⁻⁴	0.5%
5	1.00-1.30	6.0 x 16 ⁻⁶	1.06				
	1.55-1.75	6.2 x 16 ⁻⁶	1.01	5	1.55-1.75	8.0 x 10 ⁻⁵	1.06
7(3)	2.08-2:35	4.7 x 10 ⁻⁵	2.04		2.08-2.35	5.0 x 10 ⁻⁵	2.48
•	10.4-12.5	WA	HEAT-0.25°E	,	10.4-12.5	300°E	NEAT-O.5°E

⁽¹⁾ Data was obtained from the "Operations Manual, HS-001 Hultispectral Scanner," MASA; JSC-12715, April 1977.

Development of Spectral Classes A COMTAL Vision One/20, displaying a composite of channels 3, 4, and 5, in conjunction with the aerial photography, was employed to ascribe cover class labels and ground condition descriptions to line-column coordinates in the imagery in a supervised fashion. This approach was considered more appropriate than the unsupervised clustering approach, since cover classes could be defined more nearly independent of their spectral characteristics in the wavebands to be evaluated. The method used to develop training classes was of particular concern since the affect of different within-class variances for each channel by cover class on cluster class composition is not currently well understood (Bartolucci, 1978; Anuta, 1979). Once the training fields had been identified, they were grouped according to cover class. The cover class groups of training fields were then individually clustered to resolve the cover classes into a set of spectral classes. This provided training class statistics corresponding to a set of spectral classes associated with each cover class. Clustering at this stage provided a means of

⁽²⁾ Data was obtained from Salomonson, 1978.

⁽³⁾ Channel 7 (2.08-2.35 µm) was not operational at the time of the mission; all subsequent references to "channel 7" refer to the 18.4-12.5 µm waveland.

^{*}The function was generated using data obtained outside of the area from which the data for this analysis was obtained.

establishing the spectral classes on the basis of spectral variability within each cover class, but did not completely avoid the problem mentioned above. Failure to provide training statistics representing the spectral variability within each cover class was considered more deleterious to the objective of the study than clustering to obtain those classes.

Data Analysis

The mean vector and covariance matrix computed for each of the spectral classes define the individual statistical density associated with each respective spectral class. A measure of statistical distance between all pair-wise combinations of the spectral classes provides information on the "separability" of these spectral classes. This "separability" represents an a priori estimate of the probability of correct classification (Swain, Robertson, and Wacker, 1971) for measurements provided by each channel or channel combination. Only pairs of spectral classes belonging to different cover classes are of interest, since low separability between different spectral classes of the same cover class does not affect classification accuracy.

Transformed divergence was used to compute the separability. Divergence is defined as:

D =
$$f[p_1(x) - p_2(x)]$$
 in $\frac{p_1(x)}{p_2(x)}$ dx (1)

where: p₁(x) = statistical density of spectral class 1

or computationally, for the Gausian multivariate case:

$$D = \frac{1}{2} \operatorname{tr} \left[(\Sigma_{1} - \Sigma_{2})(\Sigma_{1}^{-1} - \Sigma_{2}^{-1}) \right] + \frac{1}{2} \operatorname{tr} \left[(\Sigma_{1}^{-1} + \Sigma_{2}^{-1})(m_{1} - m_{2}) \right]$$

$$(m_{1} - m_{2})^{T}$$
(2)

where: Σ is the covariance matrix and m is the mean vector associated with the respective spectral class, and

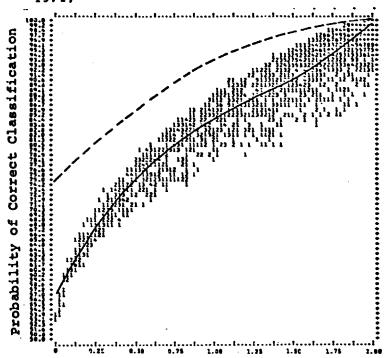
tr (trace) is the sum of the diagonal elements.

Since divergence increases without bound as the statistical distance between the two classes increases, a saturation transform is employed, resulting in a measure (i.e., transformed divergence) which corresponds more closely with percent correct classification (see Figure 1). After a certain level of statistical difference has been attained, virtually no confusion exists between the two class densities, and percent correct classification "saturates" toward 100%. The resulting transformed divergence is provided by:

$$TD = 2000 [1 - exp(-D/8)]$$
 (3)

There are some disadvantages to the use of transformed divergence as a measure of statistical difference between class densities*, but because of relative computational efficiency it is used in lieu of the alternative measures.

Figure 1. Probability of correct classification regressed against transformed divergence. (Swain et al., 1971)



Transformed Divergence

Transformed divergence (TD) values were computed for each pair of spectral classes representing different cover classes, for each channel and channel combination. These mean pair-wise TD-values were then sorted for each set of combinations involving the same number of channels. The seven channel combinations providing the highest mean pair-wise TD-values were obtained. Additional programs were written to generate summaries of the mean TD-values for each pair of cover classes (i.e., over all spectral classes representing the cover class pair) and each cover class

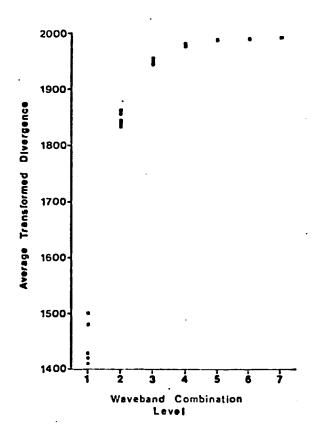
*It should be pointed out that transformed divergence is not "metric" in multivariate normal distribution functions of non-equivalent covariance matrices (Landgrebe and Wacker; 1972). That is, a pair of class densities having non-equivalent covariance matricies yet having equal mean vectors could have a transformed divergence value of zero. Also, there is no estimate for a lower confidence limit for the regression relation between transformed divergence and percent correct classification (Swain, Robertson, and Wacker; 1971).

(i.e., over all cover class pairs involving the jth cover class; j = 1, ..., 12) for these seven channel combinations.

RESULTS AND DISCUSSION

To define the optimum number of channels to use in a classification, the relationship between cost of misclassification and the probability of error must be determined. Otherwise there is no meaningful way to compare classification cost to classification accuracy. It can be observed from Figure 2 that the increase in transformed divergence (the correlate to probability of correct classification) drops off sharply after three channels, and very little is gained by using more than four channels. This result is similar to those obtained previously with the Michigan M-7, 12-channel scanner (Coggeshall and Hoffer, 1973), and the skylab 13-channel S-192 scanner (Hoffer et al., 1975). The shape of the relationship shown in Fig. 2 indicates that transformed divergence increases logarithmically as the combination level increases linearly*. The spread of the points representing the five highest ranked channel combinations for each combination level represents the difference between

Figure 2. Averaged transformed divergence for the best five waveband combinations for each combination level.



*To simplify the following discussions, "combination level" will refer to the number of channels involved in any particular set of channel combinations.

successively ranked averaged transformed divergence. As seen in Fig. 2, the mean difference between successively ranked mean separabilities decreases logarithmically as the combination level increases linearly. This implies that the rank of overall mean separability as a feature selection criterion decreases in value as the number of features comprising the selected feature subset increases.

The best combined sources of information for distinguishing between various cover classes need not have as a subset the best single source of information. This is indicated in Table 2, which shows, for example, that the single channel having the highest mean TD-value (i.e., channel 6) is not included in the 2, 3, and 4 channel combination levels having the highest mean TD-values. By comparing Table 2 with Table 3, it can be observed that the best channel or channel combination for each combination level, on the basis of mean overall separability, is not necessarily superior on a per cover class basis.

Table 2. Channel combinations, ranked by overall mean TD-value for combination levels one through six.

COMB	INATION	LEVEL
------	---------	-------

1	2	3	4	5	6
6	3,4	3,4,5	1,3,4,5	1,3,4,5,6	1,2,3,4,5,6
3	3,5	3,4,6	3,4,5,6	2,3,4,5,6	2,3,4,5,6,7
1	2,4	3,5,6	1,3,4,6	1,2,3,4,5	1,3,4,5.6,7
5	2,5	2,4,5	3,4,5,7	1,3,4,5,7	1,2,3,4,6,7
2	3,6	2,4,6	2,4,5,7	3,4,5,6,7	1,2,4,5,6,7
4	4,6	2,5,6	2,3,4,6	2,4,5,6,7	1,2,3,4,5,7
7	1,4	1,3,4	1,3,5,6	1,2,3,5,6	1,2,3,4,6,7

Table 3. Best channels and channel combinations by TD-value for each cover class. TD-value is in parentheses.

COMBINATION LEVEL

	•••••							
	1	2	3	4				
soil	3 (1820)	24 (1941)	256(1987)	1346,2346,1356(1992)				
past	6(1476)	35(1878)	345(1971)	3457 (1987)				
crop	3 (1390)	34 (1836)	345(1971)	1345(1991)				
pine	2(1435)	34(1780)	346(1912)	3456 (1960)				
pihd	2(1580)	36(1883)	356 (1982)	3456(1997)				
hdwd	3 (1688)	34(1881)	134(1933)	2346 (1952)				
sghd	3(1691)	35(1933)	346(1960)	1345,1346,2346(1972)				
tupe	6(1658)	34(1896)	245,345(1979)	2457 (1992)				
syca	5 (1753)	35 (1979)	345(1994)	1345,1346,1356(1999)				
ccut	6 (1329)	46 (1707)	356 (1889)	3456 (1947)				
mveg	4 (1270)	14(1739)	134 (1941)	1345 (1990)				
watr	5(1853)	25(1988)	246,256(1999)	1345,1346,1356(2000)				

SOIL, bare soil; PAST, pasture; CROP, row and cereal crops; PINE, pine forest; PIHD, pine-hardwood mix; HDWD, old age hardwood; SGHD, second growth hardwood; TUPE, water tupelo; SYCA, sycamore hardwood; CCUT, clearcut areas; MVEG, marsh vegetation; WATR, river water and quarry water.

Examination of the transformed divergence averaged for each cover class pair indicated that the proper selection of a single channel may provide greater separability between two cover classes than a combination of two or three channels. More specifically, the channel combination with the highest mean separability for a particular combination level does not necessarily provide a greater separability for all cover class pairs than channel combinations of a lower combination level, when the combination of the lower level is not a subset of the combination of the higher level. Examples of this relationship are: soil vs. water has a mean TD-value of 1942 in channel 6 and a mean TD-value of 1824 in channel combination 3.4; PIHD vs. CCUT has a mean TD-value of 1835 in channel 6 and a mean TD-value of 1641 in channel combination 3,4; PINE vs. MVEG has a mean TD-value of 1424 in channel 1 (the channel ranked third on the basis of mean overall TD-value) and the mean TD-value of 1182 in channel combination 3,4 (the number one ranked channel combination of all combinations involving two channels). The same relationship holds for many other cover class pairs. Such a relationship was not found when the lower level channel combination was a subset of the higher level channel combination (as would be expected).

The additional average separability achieved for each cover class, by increasing the combination level, varies greatly between cover classes and combination levels, but generally decreases logarithmically with increasing combination level. Figure 3 can be thought of as a "separability response surface." The apparent length of the lines connecting different combination levels of the same cover class is proportional to the added separability resulting from the information in the additional channel. Note that the greatest increase in separability due to the addition of the second channel occurs with second growth hardwood. As one would expect, the smallest increase in separability occurs with that cover class with the highest single channel separability (soil, in this case). It should be noted that the lines connecting the different cover classes are present merely to indicate relative differences of separability and in no way imply any functional relationship.

Figure 3 plots the maximum transformed divergence observed for each cover class in each combination level. This displays the maximum separability attainable for each cover class if the waveband combinations were selected on the basis of each cover class TD-value alone. As is clearly shown, the specific waveband combination resulting in each particular TD-value for any given waveband combination level is not constant over the different cover classes. in comparing Figures 3 and 4, it is apparent that the shapes of the curves increase in similarity with an increase in waveband combination level and are nearly identical in shape after combination level 4. This indicates that the separability by cover class provided by the best overall channel combination (Fig. 3) is nearly identical to the separability by cover class provided by the best channel combination for each individual cover class (Fig. 4) beyond waveband combination levels of 4. Thus, the best four waveband combination, based on overall transformed divergence, should provide very

close to the maximum classification accuracy for each individual cover type. However, if one were interested only in a particular cover type, high classification accuracy could be achieved using less than four channels of data.

Figure 3. Averaged transformed divergence provided by the loverall best waveband combination by waveband combination level and cover class.

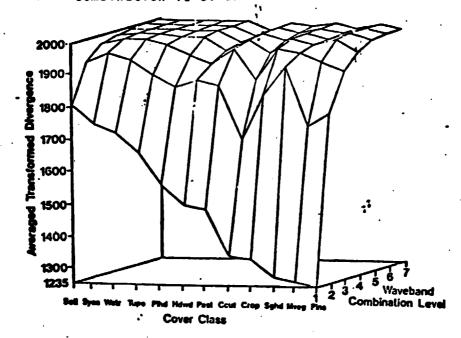
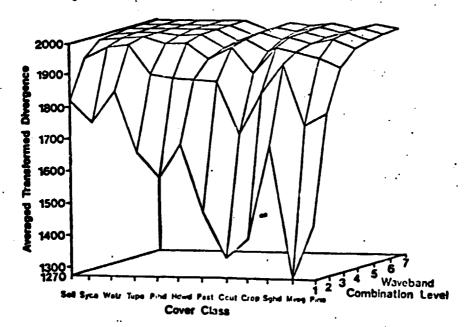


Figure 4. Averaged transformed divergence provided by the best waveband combination for leach cover class by waveband combination level and cover class.



SUMMARY AND CONCLUSIONS

Based upon the results of this study, one would not expect a computer-based classification employing more than four channels to provide much improvement in classification accuracy. The highest overall mean separability was provided by channels 1, 3, 4, and 5 (0.45-0.52, 0.63-0.69, 0.76-0.90, and 1.0-1.3 μm). This channel combination did not always provide the highest mean separability by cover class nor by pairs of cover classes. A different set of cover classes, or even a subset of the cover classes considered in this work, could result in other channel combinations yielding higher predicted classification accuracies.

Results such as these are highly data and application dependent. The conclusions pertain to channel subsets selected for classification and in no way imply that scanner systems need only obtain data in those channels in order to adequately provide remote sensory data to the various disciplines. Similar studies involving different cover classes and different seasons need to be conducted along with follow-up studies involving actual classifications.

ACKNOWLEDGEMENTS

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Appendix B - Computer Programs Developed

The following is a list of some of the programs written during the quarter June 1, 1980 - August 31, 1980. A brief description is included to assist those in need of similar code.

- WGHT2 FORTRAN Reads a file containing: 1) number of the cover classes to which a spectral class belongs, and 2) the number of pixels from each spectral class. It then computes a weight for each spectral class pair and writes a disk file of "WEIGHTS" cards within the restrictions of *SEPARABILITY. Another disk file of real variable probabilities for the occurrence of each spectral class, and the conditional probability of the occurrence of the spectral class given the occurrence of the cover class of which it is a subset.
- GRID·FTN A FORTRAN program written for the PDP-11/34 to generate a user specified grid for use in systematic sample selection on the COMTAL Vision one/20.
- DIVPRT FORTRAN A modified version of the DIVPRT subroutine called in *SEPARABILITY which is the printer output supervisor.

 This was modified to write out the class symbols and separability for each channel combination and each channel combination level, for each spectral class pair.
- SPECSEP FORTRAN Reads the disk file created by the modified DIVPRT and computes the averaged transformed divergence by cover class pair. It also sorts for and prints out the minimum TD value.
- SUMG FORTRAN Reads the disk file created by the modified DIVPRT and computes the averaged transformed divergence by cover class (i.e., for each cover class over all cover class pairs it uses the original TD; 's in order to avoid excessive rounding errors).
- CAGEN2 FORTRAN Reads a deck of COMTAL image coordinates and field descriptions; queries the user for the line-column coordinate of the first pixel displayed in terms of MIST coordinates; the run number desired on the output file; and pixel averaging if any. It then computes the MIST coordinates for each field and creates a disk file of LARS-12 card formatted records.

APPENDIX C

Tables of Averaged Transformed Divergence by Cover Class Pairs (generated by SPECSUP FORTRAN) and by cover Class (generated by SUMG FORTRAN).

Table C-1. Averaged and Minimum Transformed Divergence Values for Single Channels by Cover Class Pair.

					Cha	nnels			
			<u>6</u>	<u>3</u>	1	<u>5</u>	<u>2</u>	<u>4</u>	<u>7</u>
THE THE TENT TENT TO A PURCHANCE OF THE PURCHANCE OF THE THE TENT TO A PURCHANCE OF THE PUR	**************************************	CCUT	######################################	1778	111121121111 1111111 1111111 1 1111111 111 11111	1 1111 1111 11111 11111111 11 111 111	55000008086607774082969755 e1285682671386004750570651970 4608975 b550500008086607774082969755 e1285682671386004750570651970 4608975 b5505098225895 \$ 06267191046415922267 06506 8505098225895 \$ 06267191046415922267 06506 8505098225895 \$ 06267191046415922267 06506 850509822587 06267191111111111111111111111111111111111	5384638685871856020916657257290831819951873642477009312484652999071 597585417686878632184575704407045290359550349962728497004089578 20519584750471824369141234138786695451859157138898836489576999755 111111111111111111111111111111111	11111111111111111111111111111111111111

Table C-1. Averaged and Minimum Transformed Divergence Values for Single Channels by Cover Class Pair (cont'd.).

Minimum

Chan	nels

<u>6</u>	<u>3</u>	<u>1</u>	<u>5</u>	<u>2</u>	<u>4</u>	7
12200030020020537250754966236311114 1220006009007482 18352215 22 593 122122 1 72216 22 603 112	1139 20000 20000 20000 1045 489 277 1486 1246	102397 199919 19996 199977 1081 19509 1169 1169	3384660437191073389666492761096919687130964 5480683325394234413610322331 82181915814997 123347 2212211 4387 22331 8218191 477196 11 11	1167 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 200000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 200000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 200000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 20000 2000	1822 1315 1315 1771 477 497 497 1602 1711 407 140	466253191781745102543789631594236262306294542377556173990679949793784565691823562797353 31424316514734098 325129630723476 242165170
2375896221522963115115 60221512363115114	000005492724762999104069032005927748998021383548471753630091 000004887793084141684536485 4993981916544662344643616863719 000009 1 42 6111 15356 11 341 2218 1 08155289534326136	1900914190276156324090276127712765377876	441666644927610969 4367 223331 8215	2221ne004060e22n62868411105851 32211131209 18 274871105851 11131 1 6414871101851 11131 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	992824100127724842904950862321969990869054268507 003925408 5 60274 39457733689593209760286828298036778203131325903 1621 42 2 1 4 323137 3 3596 6 503 7 565930176994	973:53 13 13 13 13 13 13 13 13 13 13 13 13 13
9258801366150316666990766749913309 354981226858 34393643733175326527 144214 09328 2921745315721561935	95 339 1492 187 17 94 218 269 159	138 147 13584 10584 10515 15518 20662 1583 1583	891 1109 1936 188 57 481 713 740 1199	86 1478 144 1151 1671 261 440 325	1129 1305 1792 73 62 301 29 1386 569	340 172 536 342 103 186 39
1966 1381 255 880	843 40 62 161	262 466 272 1588	1996 674 80 1665	1368 145 1161 1601	1989 629 628	24 355 114 22
1231 1945 1236 196 745	1023 1134 1548 1548	46628320832071091091091091091091091091091091091091091	684 1859 866 1289 1809	1417 1772 534 1445 1740	589 1000 335 64 772	175 237 1405 175 25
1540 1540 156 156 737	1847 1847 1367 1367	1799 16 1547 1880 531	948 150 377 1882 742	1505 1557 360 1205 1497 263	5885 625 1500 1957 316	773 773 9
214 1179 1559 631 1123 1953	3563 630 1170 1319 1691	1716 1588388777 1588385777 11926 11933	8586895807225419878 658295807224819878 138778424819878 11111928	110117245067057335798404 1101473440500705735798404 1101473053442321817	1030 1113 1939 1622 1955 1994	946 27 110 1069 254 119
320 579	3 8,3	1326 577	1288 140	40 54	-400 38	577 209

Table C-2. Averaged and Minimum Transformed Divergence Values for Each of Best 2-Channel Combinations by Cover Class Pair.

					-				
			3,4	<u>3,5</u>	2,4	2,5	<u>3,6</u>	4,6	1,4
LILLLLLLLLLLTTTTTTTTTTTPPPPPPPPPPPPPPPP	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	TPHODORATGRPHODORATGREDDDPATGROODPIATGRDDDATGRDDATGRDEATGRDATGRATGRTGRATGRATGRAGRRAGRANGRAILOSUYOVARIIDSUYOVALIDSUYOVALIDSUYOVADGUYOVAGUYOVAUYOVAYOVAOVAAAAAAAAAAAAAAAAAAAAAAAA	1300000005345386000124958465267451354120156010903908057560262029054199000000534535235106839805634689594898910499768810063902140790014990000074859999797990849956948989101499799007479099001488	05000000000000000000000000000000000000	520000000400341369624894764676591252393189540903940142700600050479690000000400341369693325542396783816979067049969099890788099009991248889259797967049969099890788099009991248889259797967049969099890788099009991248882222221111111111111111111111111	44000007056433699666209704911118076518991519620568860672808760299082960000905223336996620970990199960000905223336012743079427165977419279938094000789705143037403902789600090887609999001999010000000000000000000000000	700000004300443020857490656874557d5201939905501288530985704120480896 04000000337740085966820568979481669986940960398458054680790398 9600000087855899894494879894194476952989909898458054680790398 96000000877458899894494879894194476952989905503984590997907680790398	07400000810622820125592998313483009236912026835670349769841959007185900000858179286859299831344379951659209683796387173998568999900718590000085851711111111111111111111111111111	11112222111111111111111111111111111111

Table C-2. Averaged and Minimum Transformed Divergence Values for Each of Best 2-Channel Combinations by Cover Class Pair (cont'd.).

Minimum

		•	cnanne	10		
<u>3,4</u>	3,5		2,5	<u>3,6</u>	4,6	1,4
4700000004488495349692729188557948145260338416896319271509339740376 5600000009468036440161545119392445876942859225255369266508780690381 75000000147799645626566995774258789629698972908927968780690381 11222222211 1111 111111111 1 1111 111	01000000000000000000000000000000000000	9900009021503073983304681522DE32492D640277629851300444790334019074911000099041503073944618706710174+44244229775986913200694804510170190749122212111 11111 11 111111 11 111111 12 112112	7700000502614169320140435735441612625744547650771030393102010270194540000050261416932014645316886067509259965040576026980512039016238000090542575361174023645573927744964939697400996708649034607907891222212111 11111 121111 121111 12111211	0700000001969225248637210399540677310732690306365046879701750740474 720000001969225248637210399540677310732690306365046879701750740474 7200000021666779497271976196330849922987932989780904540490474	111222222 11 11 11 11111 1 11 1 11111 1 11121 1 11121 1 11111 11111 11112	556500000241507397397689093153372840554193260785496060040828025054546990000620838267397689093153372840549806197290018305359018602808291777777777777777777777777777777777777

Table C-3. Averaged and Minimum Transformed Divergence Values for Each of Best 3-Channel Combinations by Cover Class Pair.

					CI	anners	-				
			A	<u>B</u>	<u>c</u>	D	<u>E</u>	<u>F</u>	<u>G</u>		
LULLULLILITTTTTTTTTTTPPPPPPPPPPPPPPPPPPP	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	TPRODDEATGRPEDDDEATGREDDDEATGRODDEATGRDDDEATGRDEATGRDEATGREATGREATGRATGRTRARGRR SONH WHPOUETONE WHPOUET WHPOUET WHPOUET WHPOUETH WHOO WAS A WAS TROWN WISOM WOOM WOOM WOOM WAS A WAS TROWN WOOM WOOM WOOM WOOM WOOM WOOM WOOM W	140000000000049 p7203004 00001079361538309277033007484070 690009 0010005 y6 960000099999999900000090009900099000	11220000000000000000000000000000000000	0500000042293300730520199890617078104796060050328540893907390500620 960000008998998606530490970503982050509408007056998969875900050800398 99000008998999960890990879859007594080070569989699996699660 00699	1900000099425995658210442489620897176504500170173069310908600200847970000000974259956582104424896208971765045001701730693109086002008479900000037828974594504989598206699959099006997790999099904905790099909990699	7200000017 056765995605297936109927062000904609665505575039004000955720000095990000095720000095770400095770620009599999999999999999999999999999999	4700000023577224576990142545350090100409900560838080584801400100793970000000799769559076999099900000099906999909990999999999	96000000202545&2125&65959&98577>9356660919&0000204740940900&700904786400000000002045&2125&694993385698577>9936000000000004740949900&792499499	B. C. D. E.	= 3,4,5 = 3,4,5 = 3,5,6 = 2,4,6 = 2,5,6 = 1,3,4

Table C-3. Averaged and Minimum Transformed Divergence Values for Each of Best 3-Channel Combinations by Cover Class Pair (cont'd.).

Minimum

		C	hannel	<u>5</u>				
A	B	<u>c</u>	D	<u>E</u>	<u>F</u>	<u>G</u>		
7600000099338856639405139910076555117175929450176160006709400100236720000000577962346393507594039759403975940000005776099400496040031798000000577609947999949899949699975961977908579087909000097	40000000099551481199713019454+76387694430990920040520465501370210131920000000009551481199713019454+763876995040000000520465507900380100957500000005543995909999179508895399098018959059790078090005937120000554311111111111111111111111111111111	260000003478334219346967616154739195939940030991230221607370900593 3400000012030222695599095977360797194940050549910515902370300146 970000005794979959407699769977360797194940050549910793906580900398 1122222221111111111111111111111111111	22000000000009867453429042701546399267509409873089089085560138089084712000000087914933528109537738095966881998991901475409099903050690257190000007574998773470698969439899596688199899190147540908908990790257112222222111111111111111111111111111	7600000061231476557406684438919132590405890770748799096140589060099004000000077777774655740660099004777930007709377070077007700770077007990077007990077007997	64000000911177778883170129735097934497709560670643110230404660200194 30000000894293605996047013804997349430692088083979067390094040404040 57000000077935967244605739482794779796079700995808889009404660267 112222221111111111111111111111111111	######################################	A = 3,4,5 B = 3,4,5 C = 3,5,6 D = 2,4,5 E = 2,4,6 F = 2,5,6 G = 1,3,6	5 6 5 6

Table C-4. Averaged and Minimum Transformed Divergence Values for Each of Best 4-Channel Combinations by Cover Class Pair.

Averaged

			A	<u>B</u>	<u>c</u>	D	<u>E</u>	<u>F</u>	<u>G</u>			
DOODDOOEFEE.444TT	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	TO DELIGE WOOD TOTOON WORLESTOOM WOLLSTOOM WILSTOOM WELSON WILSTOOM WILSON WILS	460000000187930638034000003090015159720500055031859037700900000300 98000000579790997098000000905099140500099079959099900990000900 9900000057979099900360000090599914050009907995909990099000000900	^90000007#4#\$07000700 0100007994#79005080000004##99769190000004## 9700000999990099700700 00009095989809000000000000909999999000000 990000999990099099	9100000001989806430890500070960484505308080000059380609004680000700 87000000489390995088090000901908858023080900705799990994009590000800 990000099999909900900090908699089090070799990990094009900000900	690000000647790986013090008040047198050109076024657035600585060099890000000099890000009999999999	680000008409703140330396930760731475705000290b36980640905150700309968000000890b5070530999900000090909090909090909090909090	\\\P\000000004\0687\0699069\0590000930065609\40800000037\9\4003\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	270000005377932234086010098033070680220904001076967000600570000004099500000579000005700000040995000003793223408600170000004099500000059790999990000080999900000809	E C D E	1 = 1,3 = 3,4 = 1,3 = 2,4 = 2,3 = 1,3	,5,6 ,4,6 ,5,7 ,5,7

Table C-4. Averaged and Minimum Transformed Divergence Values for Each of Best 4-Channel Combinations by Cover Class Pair (cont'd.).

Minimum

		<u>U</u>	nanner	2			
A	<u>B</u>	<u>c</u>	D	E	<u>F</u>	<u>G</u>	
660000000120780117997080006097956785288908009904562602849061900000166499000000776780766974009009999999999999999999999999999	33000000046572088009958500940391784407595000007080644064670066903001856700000000000708064607208800995850000090 98000000599790998958990099057992890769500009029969089890889060007999 9800000059979099885899009905799289076950000902996908989088909000799	640000009200298710620700979150695007164020010186620461905410000098695000000098647339694111111211111111111111111111111111111	130000000739540840049090097049308842969797083055563010380910050084299000000019459089990099009704930884296979708305556301038091005008849990000000739540840049090099007795039969999890299690899690899908899	560000001398806498490651460190843786100899170204160550701480600802 53000000975799999966099797947120027178620799977019969098890999900809 512222271111121111111211111211121121121	7100000001979690460430130800749197305903000990397050066809340700996 1500000003451897690130290900799258803909009900149860962903740900498 11222222111111111121121121121111111111	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	A = 1,3,4,5 B = 3,4,5,6 C = 1,3,4,6 D = 3,4,5,7 E = 2,4,5,7 F = 2,3,4,6 G = 1,3,5,6

Table C-5. Averaged and Minimum Transformed Divergence Values for Each of Best 5-Channel Combinations by Cover Class Pair.

			<u> </u>	dilliers	<u>'</u>				
	A	<u>B</u>	<u>c</u>	D	<u>E</u>	<u>F</u>	<u>G</u>		
TRENDODE AT GREED DODE AT GREDD DE AT GREDD DE AT GREDD DE AT GREDD DE AT GREAT GREA	1998 2000	9 4 00000 107 07 1090 97 00 1090 0000 0 0011 0 009 97 00 0000 0 000 0 000 0 000 0 000 0 000 0	70000000958890870051100000000000000000000000000000000	8400000079819099990150000000000000000000000000000	90000000909090909990000000000000000000	950000000000080904560500090997051105465080060000000000000715900005050000909990000000000	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	A = 1,3,4,5, B = 2,3,4,5, C = 1,2,3,4, D = 1,3,4,5, E = 3,4,5,6, F = 2,4,5,6, G = 1,2,3,5,	6 5 7 7

Best 5-Channel Combinations by Cover Class Pair (cont'd.).

Minimum

Table C-5. Averaged and Minimum Transformed Divergence Values for Each of

Cł	an	ne	ls

			MILICIA	-			
A	B	<u>c</u>	D	<u>E</u>	<u>F</u>	<u>G</u>	
370000000604380N9601109000005004N3NO33980000086846036N00749000048787000000010739017503609000043780N03398000006005N9890000099999000000999990000099999000009999	C# 000000C#0#390D#3000\405000CC0N# 000D#907 4050 00000#5# C#0CFEN# 079#09 0099 # 97 000000C#06#90E7 904509000045 084 0E 09 5070 000000459N8 0E779 C 97 #009 0099 9 99 000000#09 99 009 99 0069 C9 0000005#09 907 #09 00000N9 #89 C99 4 9 C#9 7 00 909 9 91 0000000#09 99 00 00 0000005#09 907 #09 00000N9 #89 09 9 4 9 C#9 7 00 909 9	160000009854102790520000099007590520000000007575800932007600000198650000007672902990099000000198900000007672902990099000000009999900000099990000000	730000000361660211098090005050000693658010006703833705920062900000808 76000000197490999066090009050079589779080009804497962690099090909 99000000999999069099000905071899770700009804497962690999909090909	00000008729904570790900000779779408408000090779490142804340200294 99000000899999099900900000049409000000903977000071;04650900090 990000008999999990909000004940900000090299790099999009994	1000000008748605929190300760480184001608000090819270856708110100905970000000874860592919030076048018400160800009057965006990268080005099700000905999999999999999999999	00000445733095087090977904706009055000000099995200700013500000693 95000000899899999650509999037023090780900000449490687000889900009999 960000089999999999999999	A = 1,3,4,5,6 B = 2,3,4,5,6 C = 1,2,3,4,5 D = 1,3,4,5,7 E = 3,4,5,6,7 F = 2,4,5,6,7 G = 1,2,3,5,6

Table C-6. Averaged and Minimum Transformed Divergence Values for Each of Best 6-Channel Combinations by Cover Class Pair.

		<u>A</u>	<u>B</u> <u>C</u>	D	E	<u>F</u>	<u>G</u>		
LULULULULUTTTTTTTTTTPPPPPPPPPPPPPPPPPPP	TREE CONTRACTOR FOR TWENT CONTRACTOR TO THE CONTRACTOR TWENT CONTRACTOR TW	1 N.	97.000000000000000000000000000000000000	\$\$60000000379150800006607000007805680045090000004077050077700000600 97600006099999699000069090009790517602709000008907909090990000990 976000060999999609000990099909000000790990909090	97000000000007000700000000000000000000	9:0000006094:009:00000000000000000000000	10000000 1000 1000 1000 1000 1000 1000	A = 1,2,3,4,5,6, B = 2,3,4,5,6, C = 1,3,4,5,6, E = 1,2,4,5,6, F = 1,2,3,4,5, G = 1,2,3,4,6,	,7 ,7 ,7

Table C-6. Averaged and Minimum Transformed Divergence Values for Each of Best 6-Chamel Combinations by Cover Class Pair (cont'd.).

Minimum

Ch	anı	ne.	ls

		CII	anners	2					
<u>A</u>	<u>B</u>	<u>c</u>	<u>D</u>	E	<u>F</u>	<u>G</u>			
300000004047808600030900000300555009000000000066968059900080000 94000000999084908800980000000000	7700000006070997790000090000000403183011100000004409607679047200000970000000440960767904720000097000000000000000000000000000	42000000195779047905800000000000065502409000009079776008390000009 9800000000905990990790000000010071050180900000905499900009 99000000090599099907900000000100949909000090549979099999900000	62000000055558895700099020960027056E998300700000007608400890088E0000077000000007608400890088E00000770000000770099990088E0000000000	#\$000000009444807509590904950N90717904109000000090540M960059009 \$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	440000000492670560063000000090914906106000900019580554007100000866000000099900019580554007100000866000000099990009990009990009999000099990000	4::000000519890380077090000000007290430700000009903701810001900000 670000009998790990028090000008901338903309000008709908960089990000 99000000999890990079090000089013389089090000089089099900899900000 112222222711111211221122122222211211121		B = 2,3 $C = 1,3$ $D = 1,2$ $E = 1,2$ $F = 1,2$	2,3,4,5,6 3,4,5,6,7 2,3,5,6,7 2,4,5,6,7 2,3,4,5,7 2,3,4,6,7

Table C-7. Averaged and Minimum Transformed Divergence Values for the 7-Channel Combination by Cover Class Pair.

			Ave.	Min.
SOUND SUBSTITUTE THAT THAT THE PART OF COCCOCCOCCOCCOCCOCCOCCOCCOCCOCCOCCOCCOC	のできない。これでは、これでは、これでは、これでは、これでは、これでは、これでは、これでは、	TO NOTICE AT GO PEDDD DEAT GREDDD PAT GRODD PAT GRODD AT GRODD AT GREAT	0.000000000000000000000000000000000000	# 1000000000000000000000000000000000000

Table C-8. Average Transformed Divergence Values for Each Channel by Cover Class.

Channels

	6	3	1	5	2	4	7
SACON HOUSE PROBLEM OF THE PROBLEM OF T	14726503332912 147265503332912 1472552	18497278 18497278 1849727 18696 18731 18696 18731 1863	1324644 1324644 1325508 132561 15508 1619508	12477 12477 12774 12774 1277 1275 1275 1275 1275 1275 1275	7733500 7733500 1233500 123560 121560 12179 12175	113178664 113178664 11428661 114286 117791	15777 1074 11073 11073 11075 11055 11012 11012

Table C-9. Average Transformed Divergence Values for Each of the Best Seven 2-Channel Combination by Cover Class.

	3.4	4 3,5 2,4		2,5	3,6	4,6	1,4
FOCARIA WHE CUET	2:562361962761 9:5936:53296834 9:5936:53296834 111111111111111111111111111111111111	19763993791145 18973193791145 18973791145	19424527 17775027 17775027 119723 119723 119735	787775521 9977454210563 1997454179 1997618 1997618	1034130443473 1036861754575 107686959669 11073	275654547 1877145847 177145847 1778847 1779 1779 1779	19079 20479 177021153 18802595 1797 11975

Table C-10. Averaged Transformed Divergence Values for Each of the Best Seven 3-Channel Combinations by Cover Class.

Channels

	<u>A</u>	B	<u>c</u>	D	E	<u>F</u>	<u>G</u>	A = 3,4,5
SOIL	1977 1971	1978 1960	1950 1950	19-0 1995	1754	1957	1975	B = 3,4,5
CROP PINE	1971 1903 1947	1947 1912 1980	1941 1888	1995	1925	1922	1914 1900	C = 3,5,6
OHES OHES OHES	1919 1953	1929 1950		1946 1913 1947	1915	1975 1911 1949	1955 1933 1955	D = 2,4,5
TUPE SYCA COUT	1979 1994 1870	1965 1990 1886	1957 1991 1839	1979 1974 1355	1956 1971 1880	1947 1977 1885	1940 1958 1654	E = 2,4,6
MVEG	1931 1935	1885 1997	1871 1996	1924	1994	1903	1741	$\vec{\mathbf{r}} = 2,5,6$
								G = 1,3,4

Table C-11. Averaged Transformed Divergence Values for Each of the Best Seven 4-Channel Combinations by Cover Class.

	<u>A</u>	<u>B</u>	<u>c</u>	<u>D</u>	E	F	<u>G</u>	A	= 1,3,4,5
SOIL	19 1 1 1 4 55	1990	1992 1975	19.5	1991	1992 1980	1992 1975	В	= 3,4,5,6
CRÓP PINF PIHD	1991 1951 1991	1985 1960 1997	1983 1949	1988 1939 1991	1986	1979 1950	1931 1941	C	= 1,3,4,6
HĎWD SGHO	1948 1972	1947 1956	1989 1951 1972	1941 1970	1986 1941 1965	1989 1952 1972	1991 1949 1971	D	= 3,4,5,7
TUPE SYCA CCUT	1991 1993 1943	1986 1996 1947	1984 1999 1941	1997 1997 1945	1992 1994 1998	1989 1993 1933	1975 1999 1939	E	= 2,4,5,7
WVEG WAT=	1995	1975	1989	1973	199:	1972	1994	F	= 2,3,4,6
								G	= 1,3,5,6

Table C-12. Averaged Transformed Divergence Values for Each of the Best Seven 5-Channel Combinations by cover Class.

Channels

	<u>A</u>	<u>B</u>	<u>c</u>	$\overline{\mathbf{D}}$	E	<u>F</u>	$\overline{\mathbf{c}}$	A = 1,3,4,5,6
SOIL	1995	1445	1995 1941	1997 1 9 93	1995	1994	1777	B = 2,3,4,5,6
CROP PINE PIHO	1995 1975 1999	1993 1975 1999		1996 1962 1994	1993	1993 1969 1999	1958 1965 1995	C = 1, 2, 3, 4, 5
HÓWE SGHÓ	1951 1977	1950 1975	1963 1980	j 257 197 <u>7</u>	1955 1975	1954 1972	1954	D = 1,3,4,5,7
TUPE SYCA CCUT	1995 1999 1969	1995 1998 1970	1999 2006 1962	1945	1992 1995 1977	1994 1995 1971	1998 1999 1962	E = 3,4,5,6,7
MVEG WATE	1997 2000	1994	1397	1935		1991	2000	F = 2,4,5,6,7
								G = 1,2,3,5,6

Table C-13. Averaged Transformed Divergence Values for Each of the Best Seven 6-Channel Combinations by Cover Class.

	<u>A</u>	<u>B</u>	<u>c</u>	$\overline{\mathbf{D}}$	E	<u>F</u>	<u>G</u>	A = 1,2,3,4,5,6
SOIL	1996 1995	1998 1995	1996	1998	1995 1994	1995 1995	1998 1994	B = 2,3,4,5,6,7
CROP PINE PIHD	1995 1993 1999	1998 1986 1999	1998 1979 1999	1996 1975 1947	1997 1979 2000	1976 1974 1996	1996 1975 1994	C = 1,3,4,5,6,7
HDWD SGHT TUPE	1970 1932 1999	1967 1980 1997	1965 1980 1997	1970 1932 1999	1966 1980 1999	1968 1982 1999	1970 1963 1999	D = 1,2,3,5,6,7
SYC4 CCUT	2000 1980	1999 1985	2000 1953	2000 1933	2000 1982	2000 1960	2000 1961	E = 1,2,4,5,6,7
WATE	5000	3000 1996	2000	1947	1997 2000	2000	1998 2000	F = 1,2,3,4,5,7
								G = 1,2,3,4,6,7